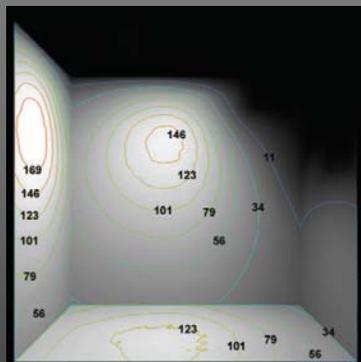


Lighting Math

NOT SO SCARY LIGHTING MATH



NOT SO SCARY LIGHTING MATH



The importance of Lighting Math:

- Calculations can determine the light levels
- Calculations can determine the required quantity of fixtures
- Calculations can verify layout

Methods to perform Lighting Math:

- By Hand
- By Computer

Lighting Math

Target Illuminance / Light Levels

Who Defines Light Levels?

- IES of North America
 - Recommended Practices
 - Defines light levels and quality of illumination by task and application
- Codes and Regulations
- The Owner



Definitions: **Task** = the work performed

Applications = the project type (i.e. School, Commercial etc,

- IESNA Light Level recommendations are for Foot-candles at the work plane (2'6" AFF)
- They have limited significance to us when we interpret the actual environment.
- Such factors as lighting walls, brightness accents, shadows, sparkle, and color have a greater influence on emotional reaction.
- IESNA's recommend light levels are for an age range of 40 – 55 years old

Orientation and simple visual tasks. Visual performance is largely unimportant. These tasks are found in public spaces where reading and visual inspection are only occasionally performed. Higher levels are recommended for tasks where visual performance is occasionally important.

A	Public spaces	30 lx (3 fc)
B	Simple orientation for short visits	50 lx (5 fc)
C	Working spaces where simple visual tasks are performed	100 lx (10 fc)

Common visual tasks. Visual performance is important. These tasks are found in commercial, industrial and residential applications. Recommended illuminance levels differ because of the characteristics of the visual task being illuminated. Higher levels are recommended for visual tasks with critical elements of low contrast or small size.

D	Performance of visual tasks of high contrast and large size	300 lx (30 fc)
E	Performance of visual tasks of high contrast and small size, or visual tasks of low contrast and large size	500 lx (50 fc)
F	Performance of visual tasks of low contrast and small size	1000 lx (100 fc)

Special visual tasks. Visual performance is of critical importance. These tasks are very specialized, including those with very small or very low contrast critical elements. Recommended illuminance levels should be achieved with supplementary task lighting. Higher recommended levels are often achieved by moving the light source closer to the task.

G	Performance of visual tasks near threshold	3000 to 10,000 lx (300 to 1000 fc)
---	--	------------------------------------

Lighting Math

Ages

**Standard Age Range
is 40-55 years old**

**Less than
40 years
old...**

*Can reduce
the light
levels up to
1/3!*



**Over 55
years old...**

*Can
increase the
light levels
up to 2/3!*

Babies require 3 times more light than a 20 year old!

IESNA Recommended Light Levels

IESNA Lighting Design Guide											Interior-1	
I. INTERIOR LOCATIONS AND TASKS	Very Important	Important	Somewhat important	Blank = Not important or not applicable								
Design Issues												
Appearance of Space and Luminaires												
Color Appearance (and Color Contrast)												
Daylighting Integration and Control												
Direct Glare												
Flicker (and Strobe)												
Light Distribution on Surfaces												
Light Distribution on Task Plane (Uniformity)												
Luminances of Room Surfaces												
Modeling of Faces or Objects												
Point(s) of Interest												
Reflected Glare												
Shadows												
Source Task/Eye Geometry												
Spurious Desirable Reflected Highlights												
Surface Characteristics												
System Control and Flexibility												
Special Considerations												
Notes on Special Considerations												
Illuminance (Horizontal)												
Category or Value (lux)												
Illuminance (Vertical)												
Category or Value (lux)												
Notes on Illuminance - see end of section												
Reference Chapter(s)												
Accounting (see Offices)												Ch. 11
Air Terminals (see Transportation Terminals in Section V, Transportation)												Ch. 23
Armories												
Art Galleries (see Museums)												Ch. 14
Auditoriums												
Assembly												
Social activity												
Banks (see Reading)												Ch. 11
Lobby												
General												
Writing area												
Tellers' stations												

Lighting Math

Summary Light Level (table 15)

TABLE 15
RECOMMENDED ILLUMINANCE VALUES

Activity	General Lighting			Task Lighting		
	Public Spaces	Simple Orientation	Occasional Visual Task	Large Visual Task	Small Visual Task	Very Small Visual Task
	3 fc	5 fc	10 fc	30 fc	50 fc	100 fc
GENERAL						
Circulation						
Corridors		•				
Elevators		•				
Lobbies			•			
Stairs		•				
Service						
Toilets and washrooms		•				
Storage						
Active			•			
Inactive		•				
HOSPITALITY FACILITIES						
Bathrooms, for grooming				•		
Bedrooms, for reading				•		
Cleaning			•			
Dining			•			
Kitchen, critical seeing					•	
Laundry				•		

Measuring Light



Luminance

- Measures how easy something is to see, or how bright a surface is – *emitting light energy*
- Examples: backlit signage, a full moon, glowing wall
- Measured in: Foot-Lamberts (US) or Candelas per meter squared (metric)
1 Foot-Lambert = 3.426 Candelas/m²

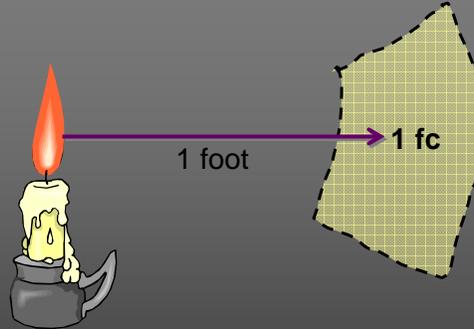


Illuminance

- Measures how much light there is to see by, the light level to perform a task – *arriving lighting energy*
- Examples: emergency light level on the floor,
- Measured in: Foot-Candles (US) and Lux (Metric)

Lighting Math

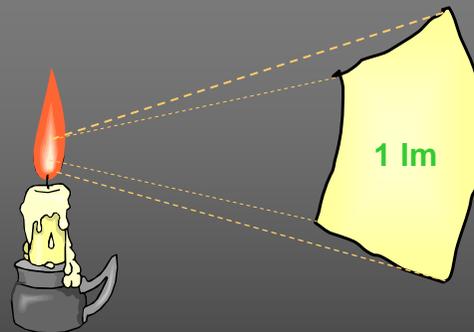
Light – The Foot-candle



Foot-candle is known as a unit of light - direct illumination light level

Derived from one candle placed at a distance of one foot from a surface is defined as a **foot-candle** (abbreviation = fc or FC)

Light – The Lumen



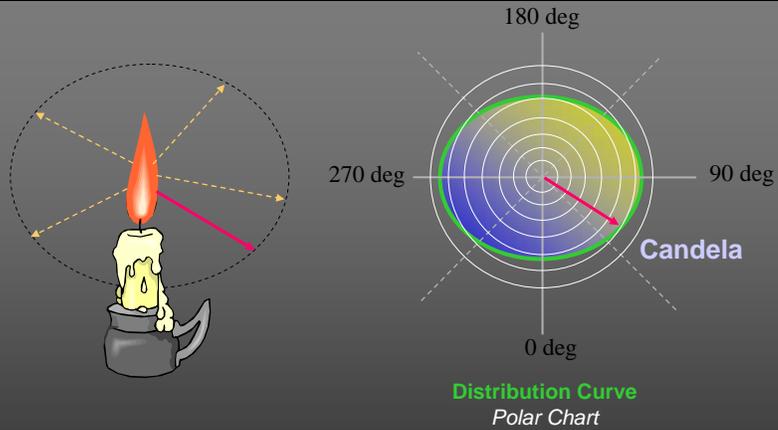
The energy of light from a candle falling on a one foot square **area** is **One Lumen** (abbreviation = lm)

*The total amount of light energy coming out of the **candle** is approximately 13 lumens
The total amount of light energy coming out of 100-watt A-lamp is approximately 1650 lumens*

NOT DEFINED BY DISTANCE

Lighting Math

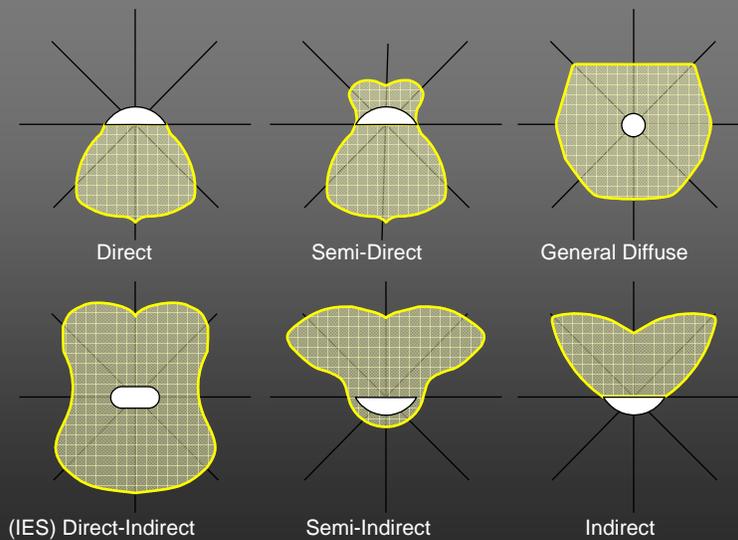
Light – The Candela



Candle Power is the intensity value at any given direction.
(unit is Candela, abbreviated as cp)

Distribution Curve represents the total light intensity pattern produced by a source

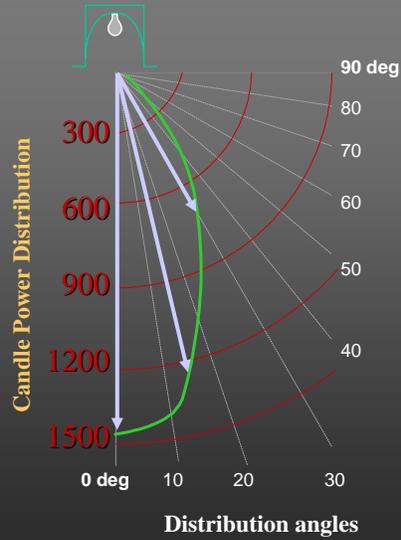
CIE Luminaire Types / Distributions



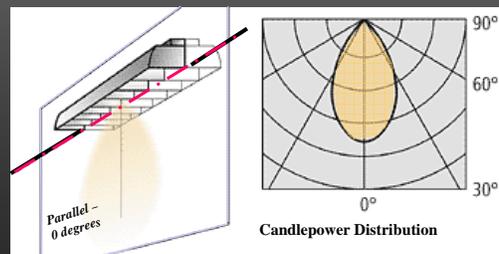
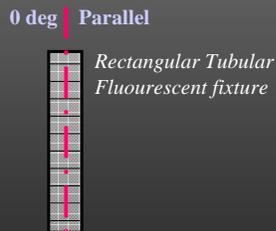
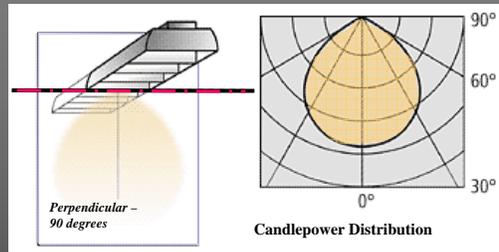
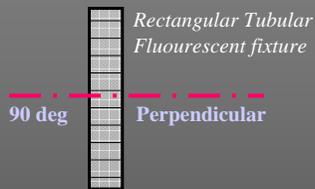
Lighting Math

Candlepower Distribution Curve

- **Candlepower distribution curves** provides intuitive information on how a **luminaire** will perform
- **Candela** values are used in calculations to predict light levels



Asymmetrical Distribution Curve



Lighting Math

Light Measurement

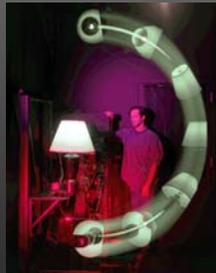
Measures the candlepower distribution of a particular lamp or luminaire.

Information is generated in a -- **Photometric report**



Erik is setting up a lamp for testing in the 2m integrating sphere.

Integrating Sphere



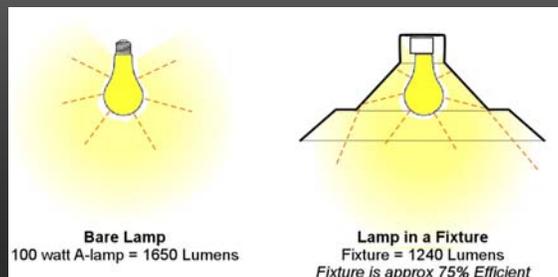
Gonio-Photometer



The Spectro-Radiometer

Lumens versus Candelas

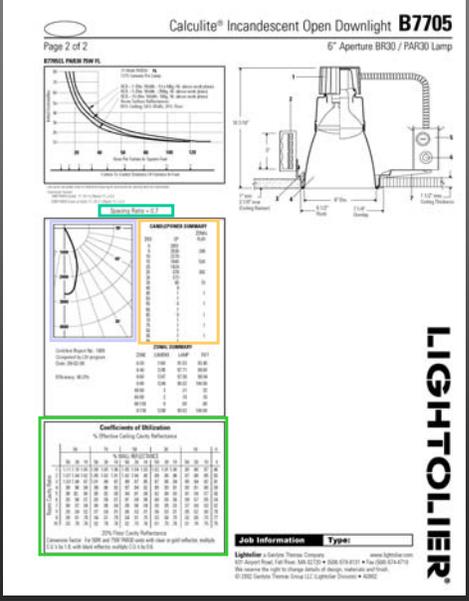
- **Lumen** is an amount of **ENERGY**
- **Candela** is an amount of **INTENSITY**
- Light output from lamps and fixtures be measured in **Lumens** and **Candelas**.
- Fixtures alter **Lumen** and **Candela** output (Their values can only be found in Photometry Reports)



Lighting Math

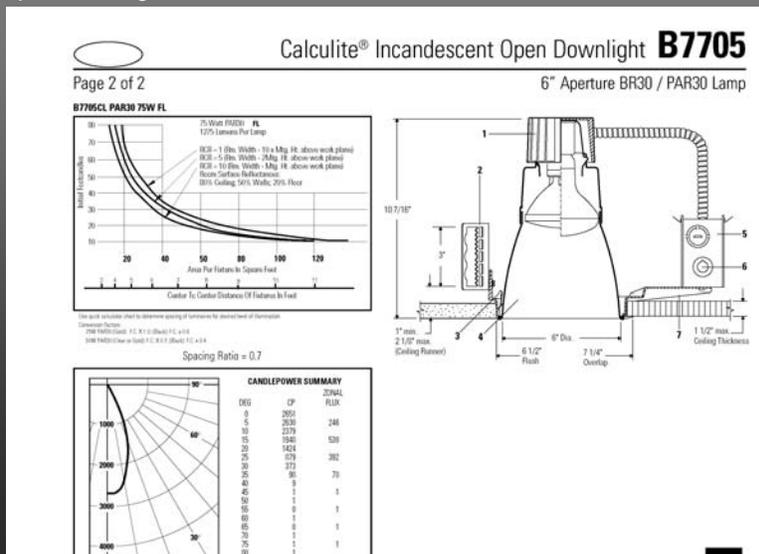
Photometry Reports

- Plot of candlepower values
- Summary of candlepower values in different planes
- Fixture Efficiency
- Lumen Summary
- Luminance summary
- Spacing criteria (SC) or Spacing/Mounting Height (S/MH) for uniformity
- Coefficient of Utilization Table
- Guides



Photometry Reports: sample 1

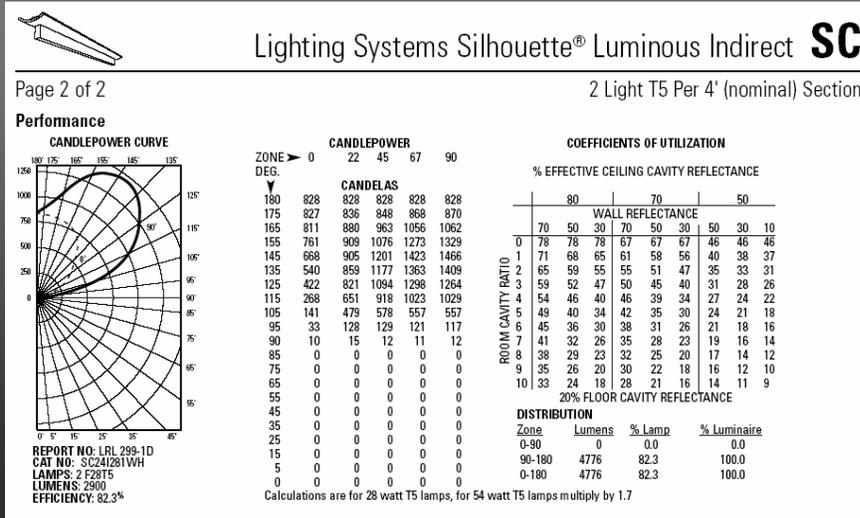
- Open Downlight



Lighting Math

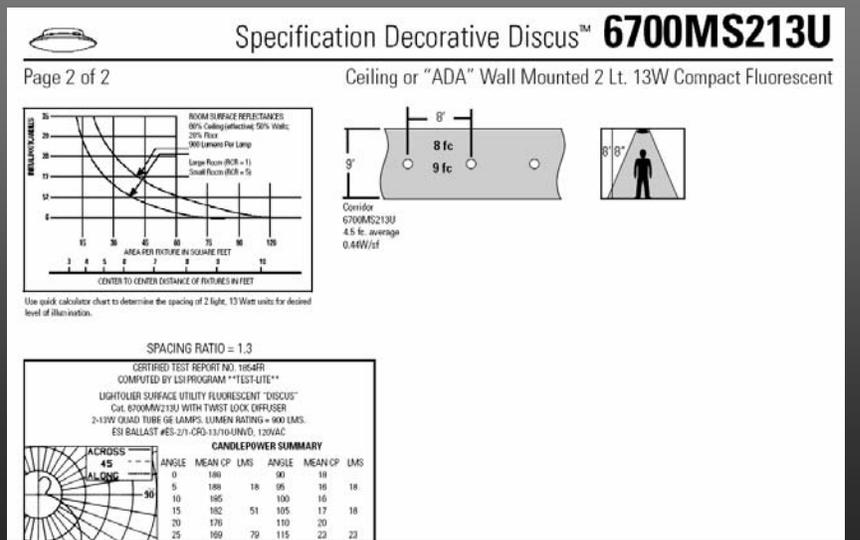
Photometry Reports: sample 2

- Indirect Pendant



Photometry Reports: sample 3

- Ceiling Fixture



Lighting Math

Hand Methods to Calculate Light

Mnfrs Guides

- Direct or Average Illumination from a Fixture or Lamp
- Recommended spacing or layout

Point-by-Point

- Direct light level from a Fixture or Lamp

Lumen Method

- Average Light Level in a Room from a Fixture
- Can be used to determine quantity needed

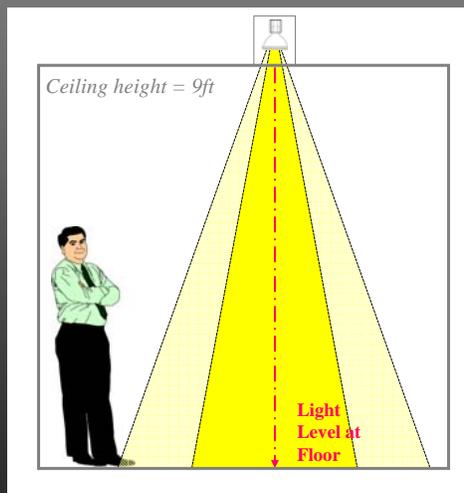
Point-by-Point

$$\text{Foot-candle} = \frac{\text{Candle Power}}{\text{Distance}^2}$$

$$\text{FC} = 2651 \text{candelas} / 9\text{ft}^2$$

$$\text{FC} = 2651 / 81$$

$$\text{FC} = 32.7 \text{ foot-candles}$$



PHOTOMETRIC DATA

Beam Angle (°)	Beam Diameter (ft)	Beam Area (sq ft)	Beam Diameter (m)	Beam Area (sq m)
10	1.5	2.25	0.457	0.209
15	2.25	5.06	0.688	0.471
20	3.0	9.00	0.914	0.836
25	3.75	14.06	1.143	1.307
30	4.5	20.25	1.372	1.880
35	5.25	27.56	1.601	2.554
40	6.0	36.00	1.830	3.330
45	6.75	45.56	2.059	4.234
50	7.5	56.25	2.288	5.260
55	8.25	68.06	2.517	6.427
60	9.0	81.00	2.746	7.726
65	9.75	95.56	2.975	9.157
70	10.5	111.75	3.204	10.720
75	11.25	129.56	3.433	12.414
80	12.0	148.00	3.662	14.237
85	12.75	168.06	3.891	16.190
90	13.5	189.75	4.120	18.273

SPACING RATIO = 0.7

ILLUMINATION SUMMARY

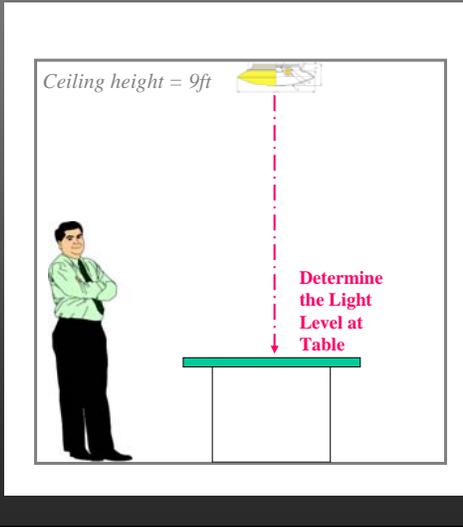
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50	7.5	56.25	2.288	5.260
55	8.25	68.06	2.517	6.427
60	9.0	81.00	2.746	7.726
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Lighting Math

Point-by-Point

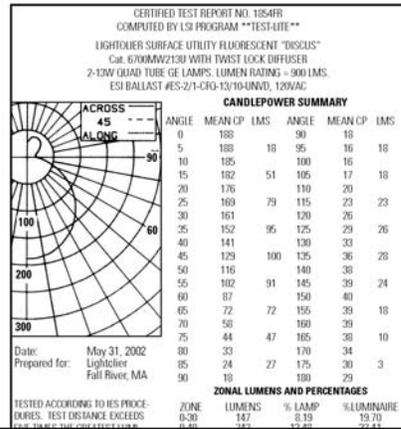
$$\text{Foot-candle} = \frac{\text{Candle Power}}{\text{Distance}^2}$$

- Ceiling Fixture Example



$$\text{FC} = \frac{\text{candelas}}{\text{ft}^2}$$

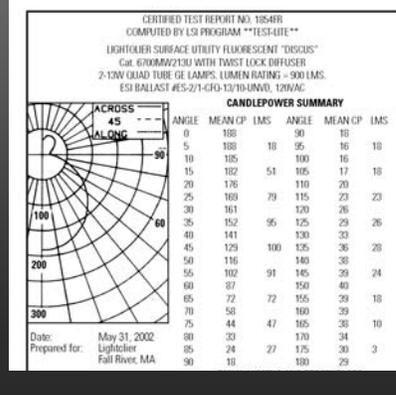
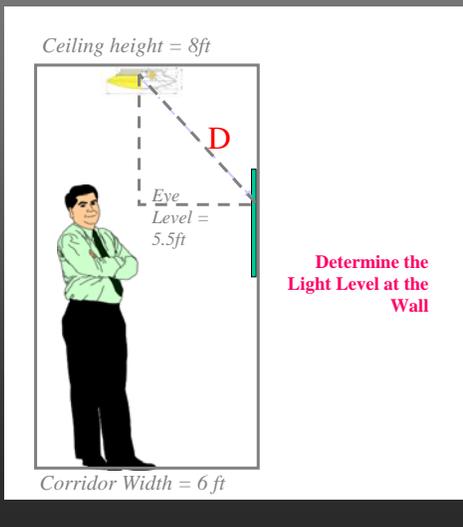
$$\text{FC} = \text{foot-candles}$$



Point-by-Point

$$\text{Foot-candle} = \frac{\text{Candle Power}}{\text{Distance}^2}$$

- Ceiling Fixture Example

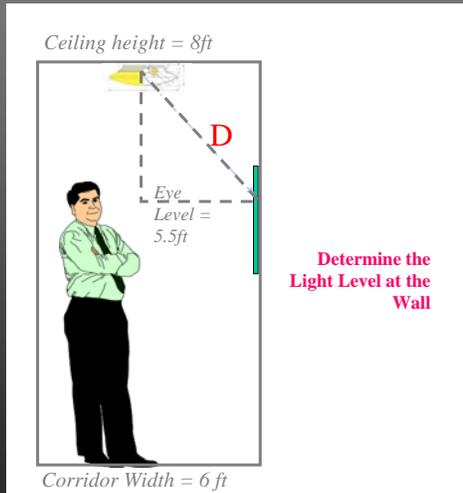


Lighting Math

Point-by-Point

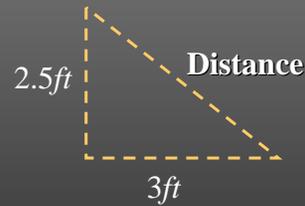
$$\text{Foot-candle} = \frac{\text{Candle Power}}{\text{Distance}^2}$$

- Ceiling Fixture Example



To solve for **D**, you can:

- Scale the Drawing, or
- Use Trigonometry



$$A^2 + B^2 = C^2$$

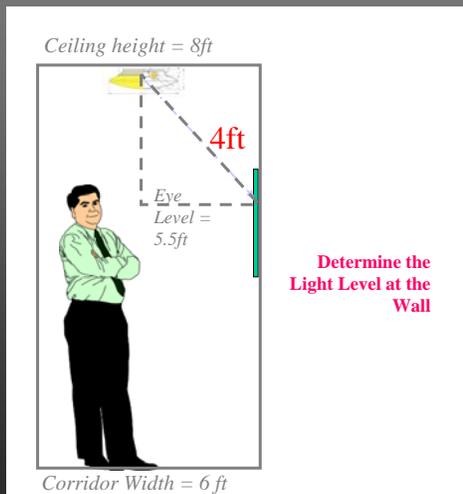
$$2.5^2 + 3^2 = C^2 \quad C = \sqrt{6.25 + 9}$$

$$6.25 + 9 = C^2 \quad C = 3.9 \text{ (approx 4ft)}$$

Point-by-Point

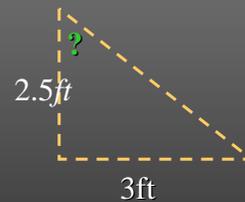
$$\text{Foot-candle} = \frac{\text{Candle Power}}{\text{Distance}^2}$$

- Ceiling Fixture Example



To solve for **Angle**, you can:

- Scale the Drawing, or
- Use Trigonometry



$$\text{Tan (Angle)} = \text{Opp} / \text{Adj}$$

$$\text{Angle} = \text{Tan}^{-1} (\text{Opp} / \text{Adj})$$

$$\text{Angle} = \text{Tan}^{-1} (3 / 2.5)$$

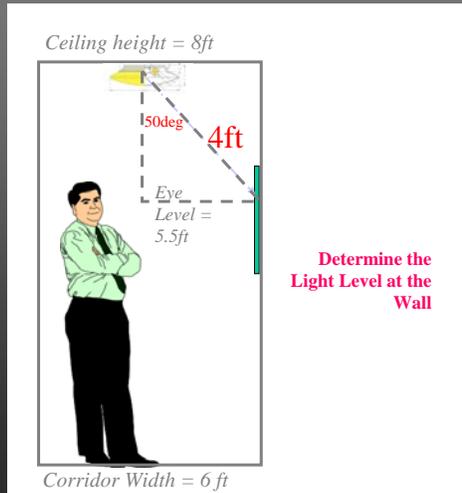
$$\text{Angle} = 50 \text{ degrees}$$

Lighting Math

Point-by-Point

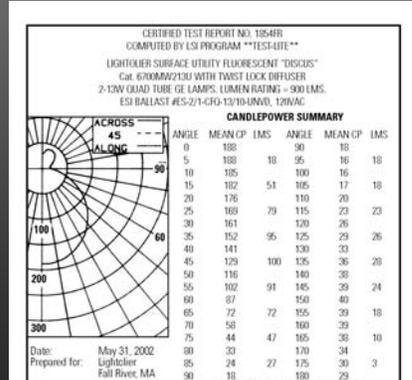
$$\text{Foot-candle} = \frac{\text{Candle Power}}{\text{Distance}^2}$$

- Ceiling Fixture Example



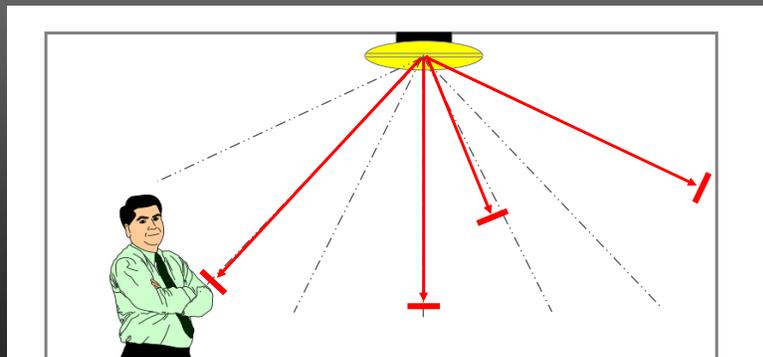
$$\text{FC} = \frac{\text{candelas}}{\text{ft}^2}$$

$$\text{FC} = \text{foot-candles}$$



Point-by-Point Factors

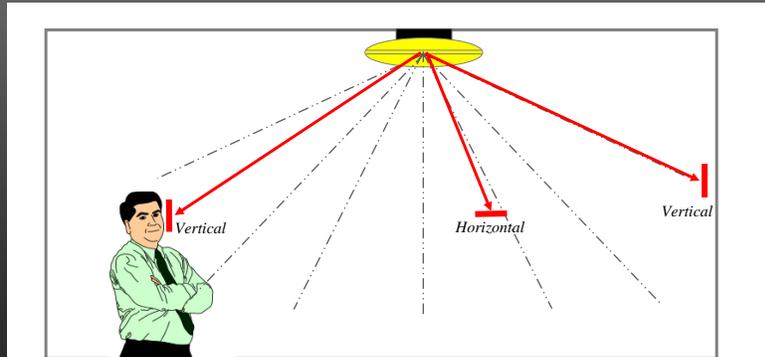
- Calculated Levels are Facing the Light Fixture
 - With the exception of directly below



Lighting Math

Point-by-Point Factors

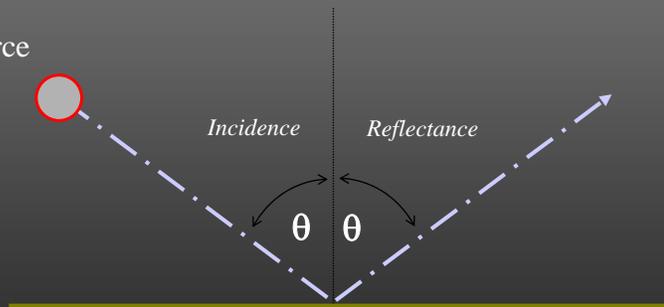
- You need to factor an adjustment if you want levels at other angles (IE Horizontal, Vertical Angles)
 - **COSINE Adjusted!!**



COSINE Adjustments

$$\text{Foot-candle} = \frac{\text{Candle Power}}{\text{Distance}^2} \times \text{COS}(\text{Angle of Incidence})$$

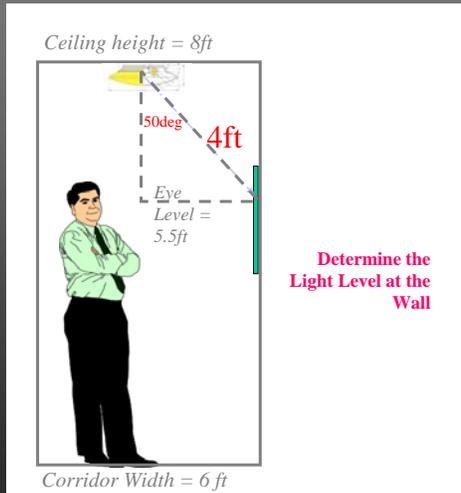
Light Source



Lighting Math

Point-by-Point... with COSINE Adjustment

- Ceiling Fixture Example



$$FC = CP/D^2 \times \text{COS}(\text{angle})$$

What is the Angle of Incidence?

$$FC = 7.25 \times \text{COS}(\text{ ___ deg})$$

$$FC = \text{ ___ foot-candles}$$

Methods to Calculate Light

Point-by-Point

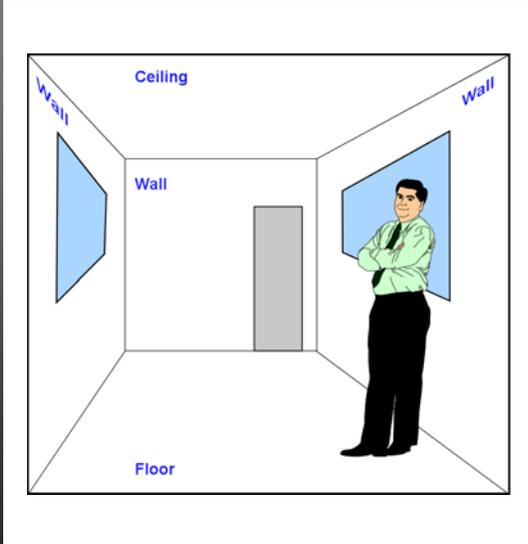
- Direct Illumination from a Fixture or Lamp
 - You need...
 - Photometry
 - Distances from Fixture or Lamp

Lumen Method

- Average Light Level in a Room from a Fixture
 - You need...
 - Photometry
 - Room Dimensions and Surface Reflectance's

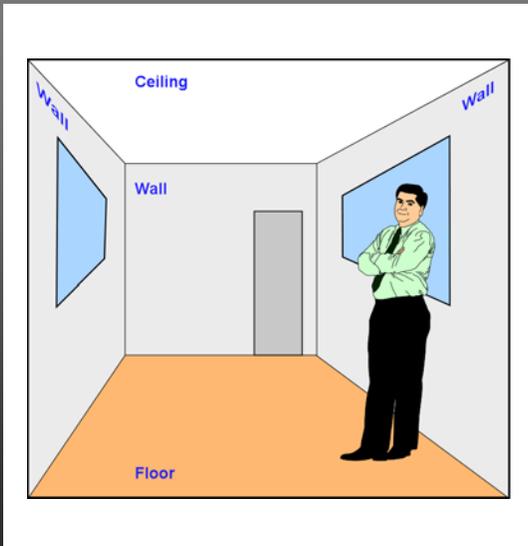
Lighting Math

Room Reflectance



- Room comprised of Walls, Ceiling, and Floor.
- Walls typically have Doors and Windows
- All surfaces have a reflectance value to bounce light.
- Light from Light Fixture bounces off of all surfaces.

Room Reflectance



- Surfaces with less reflectance will bounce less light
- Typical Reflectance Values:
 - 75%-90% White, Off White, Grey, Light tints of Blue or Brown
 - 30%-60% Medium Green, Yellow, Brown, or Grey
 - 10%-20% Dark Grey, Medium Blue
 - 5%-10% Dark Blue, Brown, Dark Green, and many wood finishes

Lighting Math

Calculations using Lumens

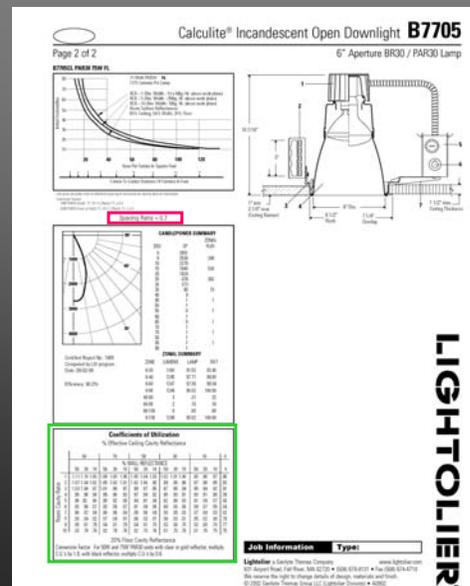
- Lumen Method Calculation

- Calculates the **Average Illumination** for a room.
- Takes into account the room surface reflectance's – but assumes the surfaces are diffuse (not shiny!).
- Assumes an empty room (without furniture).
- Can also be used to **determine the required Quantity of Fixtures** needed for a target light level.
- Does not determine light fixture layout or location – you must following mnfrs spacing criteria.

1. You need Room Dimensions and the Fixture Mounting Height.
2. You need to select a Light fixture
3. Determine the rooms Room Cavity Ratio (RCR).
4. Look-up the fixtures Coefficient of Utilization for the RCR.
5. Calculate!

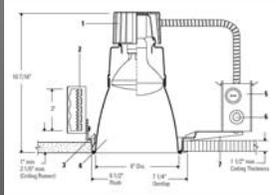
Photometry Reports

- Plot of candlepower values
- Summary of candlepower values in different planes
- Fixture Efficiency
- Lumen Summary
- Luminance summary
- Spacing Criteria (SC) or Spacing/Mounting Height (S/MH) for uniformity
- Coefficient of Utilization Table
- Guides



Lighting Math

Coefficient of Utilization



Coefficients of Utilization
% Effective Ceiling Cavity Reflectance

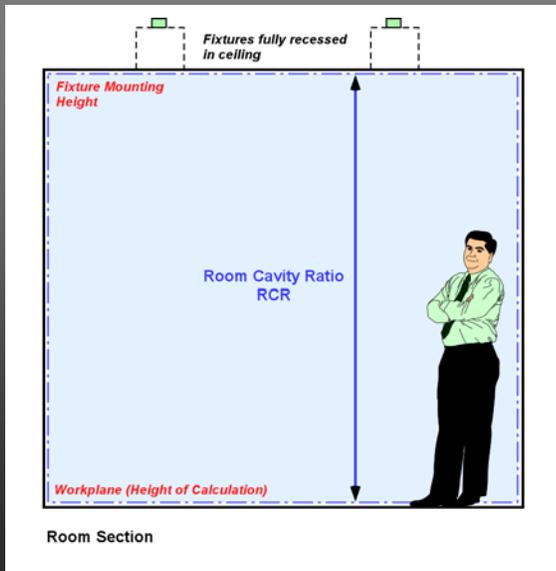
Room Cavity Ratio	% WALL REFLECTANCE											
	90		70		50		30		10		0	
1	1.11	1.10	1.09	1.08	1.07	1.06	1.05	1.04	1.03	1.02	1.01	1.00
2	1.07	1.04	1.02	1.01	1.00	0.99	0.98	0.97	0.96	0.95	0.94	0.93
3	1.03	1.00	0.97	0.95	0.93	0.91	0.89	0.87	0.85	0.83	0.81	0.79
4	0.99	0.96	0.94	0.92	0.90	0.88	0.86	0.84	0.82	0.80	0.78	0.76
5	0.96	0.92	0.90	0.88	0.86	0.84	0.82	0.80	0.78	0.76	0.74	0.72
6	0.93	0.89	0.87	0.85	0.83	0.81	0.79	0.77	0.75	0.73	0.71	0.69
7	0.90	0.87	0.84	0.82	0.80	0.78	0.76	0.74	0.72	0.70	0.68	0.66
8	0.88	0.84	0.82	0.80	0.78	0.76	0.74	0.72	0.70	0.68	0.66	0.64
9	0.85	0.81	0.79	0.77	0.75	0.73	0.71	0.69	0.67	0.65	0.63	0.61
10	0.83	0.79	0.76	0.74	0.72	0.70	0.68	0.66	0.64	0.62	0.60	0.58

20% Floor Cavity Reflectance
Conversion Factor: For 50W and 75W PAR30 units with clear or gold reflector, multiply C.U.'s by 1.0; with black reflector, multiply C.U.'s by 0.6.

- Also known as **CU**
- Defines the percentage of light output that is expected from a fixture
- The value is determined by a CU table
- For commercial Reflectance of **80/50/20**, the actual CU value is this.

Room Cavity Ratio

$$RCR = \frac{5 \times MH \times (L+W)}{\text{Room Area}}$$

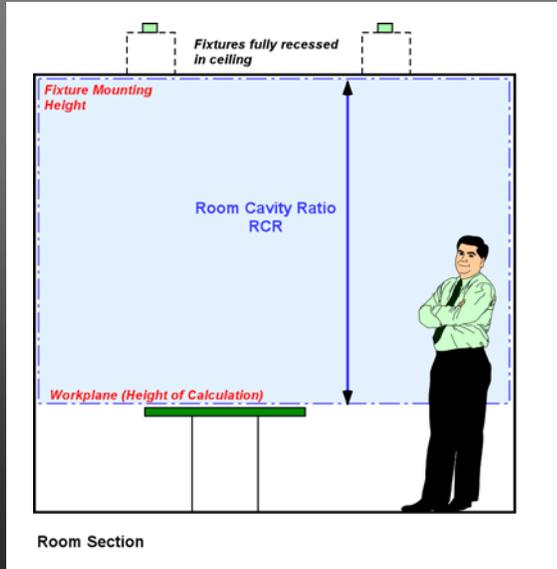


- The **RCR** can vary depending on the height you want to calculate... **as shown here with the calculation height at the floor.**

Lighting Math

Room Cavity Ratio

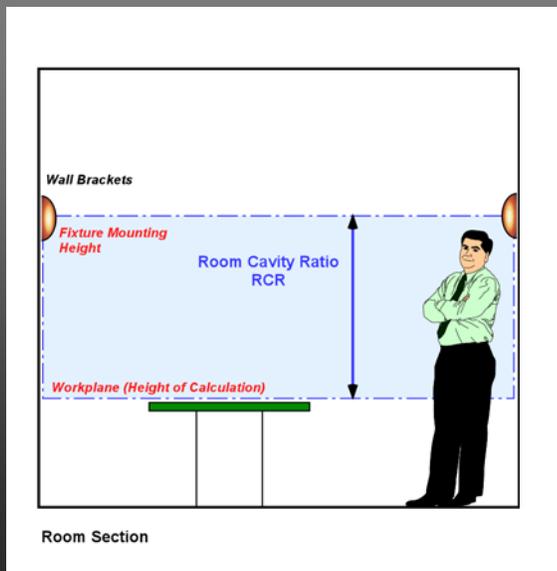
$$RCR = \frac{5 \times MH \times (L+W)}{\text{Room Area}}$$



- Room Cavity Ratio (aka **RCR**) is the volume between the **Fixture** and **Height of Calculation**
- Workplane height is typically 30-inches above the floor
- A rooms RCR will always be between 1 and 10

Room Cavity Ratio

$$RCR = \frac{5 \times MH \times (L+W)}{\text{Room Area}}$$

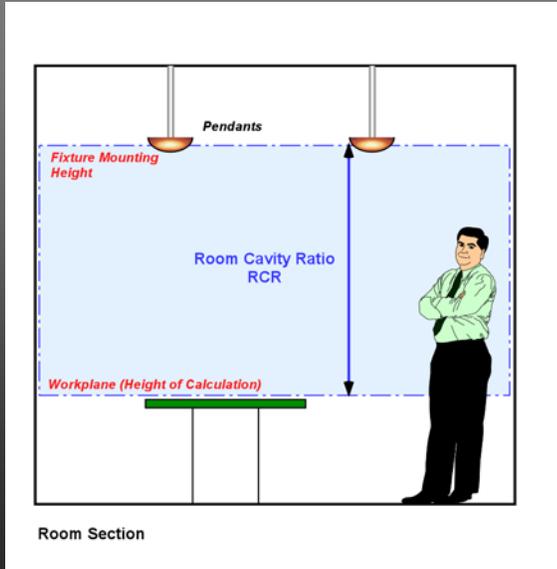


- The **RCR** can vary depending on the height of the fixture....*as shown here with Wall Brackets or Sconces.*

Lighting Math

Room Cavity Ratio

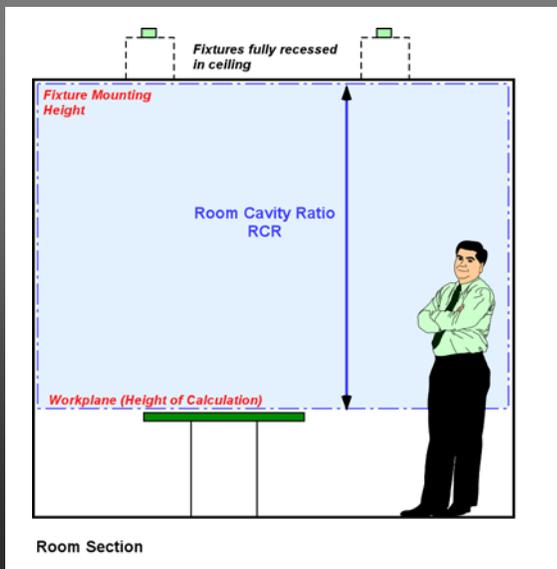
$$RCR = \frac{5 \times MH \times (L+W)}{\text{Room Area}}$$



- The **RCR** can vary depending on the height of the fixture....**as shown here with Pendants.**

Room Cavity Ratio

$$RCR = \frac{5 \times MH \times (L+W)}{\text{Room Area}}$$



Example:

Room Width: 12ft
 Room Length: 15ft
 Ceiling Height: 10ft

$$RCR = \frac{5 \times (\quad) \times (\quad + \quad)}{(\quad \times \quad)}$$

RCR =

Lighting Math

Lumen Method Formula

To Calculate Foot-candle level:

$$FC = \frac{\text{Qty of Fixtures} \times \text{Number of Lamps per Fixture} \times \text{Lumens per Lamp} \times CU}{\text{Area of the Room}}$$

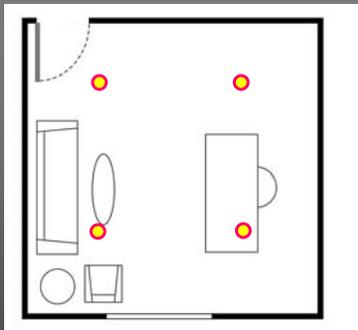
To Calculate number of Fixtures:

$$FC = \frac{\text{Total Lumens in the Room} \times CU}{\text{Area of the Room}}$$

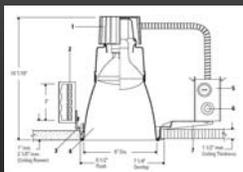
$$\text{Qty of Fixtures} = \frac{FC \times \text{Area of the Room}}{\text{Number of Lamps per Fixture} \times \text{Lumens per Lamp} \times CU}$$

$$\text{Qty of Fixtures} = \frac{FC \times \text{Area of the Room}}{\text{Total Lumens in the Room} \times CU}$$

Lumen Method Example 1



What is the resulting Foot-candle Level at table height from four downlights?



Example:
 Room Width: 12ft
 Room Length: 15ft
 Ceiling Height: 10ft

Lumen Method Calculation

Project: _____
 Room/Area: _____

Room Cavity Ratio:
 Room Width (W): _____
 Room Length (L): _____
 Fixture Mtg Height (MH): _____
 $RCR = \frac{5 \times (MH) \times (L + W)}{L \times W}$
 $RCR = 5 \times () \times () \times (+)$
 $RCR =$ _____
 Irregular Room
 $RCR = \frac{2.5(MH) \times (Perimeter Length)}{Area}$

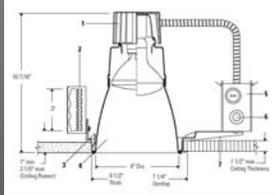
Calculation:
 Fixture Description: _____ CU: _____
 Lamp: _____ Lumens per Fixture: _____ Lumens per Lamp: _____

$FC = \frac{(\text{Qty of Fixtures}) \times (\text{Lumens per Lamp}) \times (\# \text{ of Lamps per Fixture}) \times CU \times MF}{L \times W}$
 $FC = () \times () \times () \times () \times ()$
 $FC =$ _____

$\text{Qty of Fixtures} = \frac{FC \times L \times W}{(\text{Lumens per Lamp}) \times (\# \text{ of Lamps per Fixture}) \times CU \times MF}$
 $\text{Qty of Fixtures} = \frac{() \times () \times ()}{() \times () \times () \times ()}$
 $\text{Qty of Fixtures} =$ _____

Lighting Math

Coefficient of Utilization



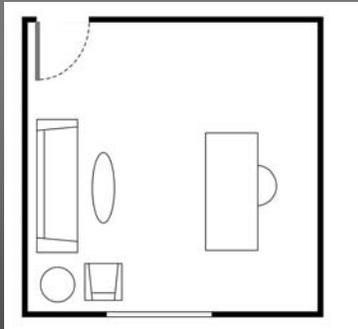
Coefficients of Utilization
% Effective Ceiling Cavity Reflectance

Room Cavity Ratio	% WALL REFLECTANCE															
	50	30	10	50	30	10	50	30	10	50	30	10	0			
1	1.11	1.10	1.00	1.09	1.00	1.06	1.05	1.04	1.03	1.02	1.01	1.00	30	36	37	36
2	1.07	1.04	1.02	1.05	1.03	1.01	1.02	1.00	98	99	98	96	97	96	95	93
3	1.03	1.00	97	1.01	99	97	99	97	95	97	95	94	95	94	92	91
4	99	96	94	99	96	93	97	94	92	95	93	91	93	91	90	89
5	96	92	90	95	92	89	94	91	89	92	90	88	91	89	87	86
6	93	89	87	93	89	87	91	89	86	90	88	86	89	87	85	84
7	89	87	84	90	86	84	89	86	84	88	85	83	87	84	83	82
8	86	84	82	87	84	81	86	83	81	86	83	81	85	82	80	79
9	83	81	79	84	81	79	84	81	79	83	80	78	82	80	78	77
10	83	79	76	82	79	76	82	79	76	81	78	76	81	76	75	75

20% Floor Cavity Reflectance
Conversion Factor: For 50W and 75W PAR30 units with clear or gold reflector, multiply C.U.'s by 1.0; with black reflector, multiply C.U.'s by 0.6.

- Also known as **CU**
- Defines the percentage of light output that is expected from a fixture
- The value is determined by a CU table
- For our example:
- RCR _____
- the CU is _____
- For commercial Reflectance of **80/50/20**, the actual CU value is this.

Lumen Method Example 2



How many fixtures do I need to achieve 30-foot-candles at table height?



Lumen Method Calculation

Project: _____
Room/Area: _____

Room Cavity Ratio:
Room Width (W): _____
Room Length (L): _____
Fixture Mtg Height (MH): _____

$RCR = \frac{5 \times (MH) \times (L + W)}{L \times W}$

$RCR = 5 \times () \times () \times ()$

RCR = _____

Irregular Room
 $RCR = \frac{2.5(MH) \times (Perimeter Length)}{Area}$

Calculation:
Fixture Description: _____ CU: _____
Lamp: _____ Lamps per Fixture: _____ Lumens per Lamp: _____

$FC = \frac{(Qty \text{ of Fixtures}) \times (Lumens \text{ per Lamp}) \times (\# \text{ of Lamps per Fixture}) \times CU \times MF}{L \times W}$

$FC = () \times () \times () \times () \times ()$

FC = _____

$Qty \text{ of Fixtures} = \frac{FC \times L \times W}{(Lumens \text{ per Lamp}) \times (\# \text{ of Lamps per Fixture}) \times CU \times MF}$

Qty of Fixtures = _____

Qty of Fixtures = _____